**Midterm 1 Practice for COMP 6321 Fall 2019**

**– Extensions**

The questions in this practices midterm are suggestive only of the style and difficulty of questions that will be asked on on the real midterm. The length and the particular course content evaluated will be different.

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| Q1. [10 marks] This question is about logistic regression models |
| a) [2 marks] What kind of learning task is logistic regression used for? |
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| b) [1 mark] Can the optimal parameter vector w for a logistic regression problem be solved for ‘directly’? |
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| c) [2 marks] Is the decision boundary of logistic regression linear or non-linear within the feature space Φ? |
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| d) [3 marks] Assume you are given data set { (x1, y1), (x2, y2), … (xN, yN) }. Write the logistic regression loss function with respect to this data set. For full marks include the feature transformation Φ(.) . |
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| e) [2 marks] Assume you are given training set in matrix format where X and y are:  Plot the data in two dimensions and draw the decision boundary that would result from applying logistic regression. Be sure to indicate which side corresponds to predicting y = 1. |
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| Q2. [10 marks] Assume we have samples {x1, x2, …, xN} from a univariate normal distribution 𝒩(μ, σ). The likelihood p(x | μ, σ) having observed a single point x is therefore |
| a) [2 marks] The likelihood is a function of which variable(s)? |
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| b) [2 marks] Write the likelihood p(x1, …, xN) having observed all xi jointly. |
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| c) [2 marks] Write the negative log likelihood of p(x1, …, xN | μ, σ). |
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| d) [2 marks] Write the gradient of the negative log likelihood of p(x1, …, xN | μ, σ). |
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| e) [2 marks] Use your answer from part (d) to derive a maximum likelihood estimate of the normal distribution parameters. |
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| Q3. [8 marks] This question is about programming machine learning concepts with Numpy. You can assume that import numpy as np has already been run. |
| a) [2 marks] You are given the following incomplete function:  def linear\_model\_predict(X, w):  “””  Returns predictions from linear model y(X, w) at each point X[i, :] using parameters w.  Given X with shape (N,D+1) and w must have shape (D+1,), and return result will have shape (N,).  “””  Complete the function in the space below. (No need to copy the above function signature.) For full marks, your answer should be fully vectorized. |
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| b) [2 marks] You are given the following incomplete function:  def sigmoid(z):  “””  Return the element-wise logistic sigmoid of array z.  “””  Complete the function in the space below (No need to copy the above function signature.) For full  marks, your answer should be fully vectorized. |
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| c) [4 marks] You are given the following incomplete function:  def linear\_regression\_by\_gradient\_descent(X, y, w\_init, learn\_rate=0.05, num\_steps=500):  “””  Fits a linear model by gradient descent.  If the feature matrix X has shape (N, D), the targets y should have shape (N,)  and the initial parameters w\_init should have shape (D,).  Returns a new parameter vector w that minimizes the squared error to the targets.  “””  The gradient of a linear model can be expressed mathematically as  𝓁LS  Complete the function in the space below. |
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| d) [4 marks] You are given the following incomplete function:  def linear\_regression\_by\_direct\_solve(X, y):  “””  Fits a linear model by directly solving for the optimal parameter w.  “””  The gradient of a linear model can be expressed mathematically as  𝓁LS  Complete the function in the space below. |
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| e) [4 marks] You are given the following incomplete function:  def logistic\_model\_predict(X, w):  “””  Returns predictions from logistic model y(x, w) at each point X[i, :] using parameters w.  Given X with shape (N, D+1), w must have shape (D+1,) and the result will have shape (N,).  “””  Complete the function in the space below. |
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| f) [4 marks] You are given the following incomplete function:  def logistic\_regression\_grad(X, y, w):  “””  Returns the gradient for basic logistic regression.  “””  The basic logistic regression training objective is:  𝓁LR(**w**)  Complete the function in the space below. |
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| g) [4 marks] You are given the following incomplete function:  def logistic\_regression(X, y, w\_init, learn\_rate=0.05, num\_steps=500):  “””  Fits a logistic model by gradient descent.  If the feature matrix X has shape (N,D), the targets y should have shape (N,) and the initial parameters w\_init should have shape (D,).  Returns a new parameter vector w that minimizes the negative log likelihood of the targets  “””  The basic gradient for the above training objective is:  𝓁LR(**w**)  Complete the function in the space below. |
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| Q4. [6 marks] This question is about the assigned reading: the 2001 paper by Leo Breiman. |
| a) [2 marks] After having worked as a consultant, what were Breiman’s “perceptions” about how to work with data? |
| *(section 3.3 Perceptions on Statistical Analysis)*  (a) Focus on finding a good solution  (b) Live with the data before you plunge into modeling  (c) Search for a model that gives a good solution, either algorithmic or data model  (d) Predictive accuracy on test sets is the criterion for how good the model is  (e) Computers are an indispensable partner |
| b) [1 marks] How was predictive accuracy measured in Breiman’s “Ozone project”? |
| *(section 3.1 The Ozone Project)*  In the project, he set f(x) is an accurate predictor of the next day’s ozone level. He used the first five years of data as the training set, and the last two years as a test set. And large linear regressions were run, followed by variable selection. The retained variables were added together as the prediction of the next day’s ozone level, compared with the real next day’s ozone level. |
| c) [2 marks] Describe the modeling approach that Breiman’s team used in the “Chlorine project” |
| *(section 3.2 The Chlorine Project)*  In the project, predictor vector **x** is of variable dimensionality from 30 to 10,000. Breiman’s team randomly divided the data set into a 25,000 member training set and a 5,000 member test set. After that, they applied the decision tree algorithm by the design of the huge set of yes-no questions applied to a mass spectra of any dimensionality. And they got 95% accuracy. |
| d) [2 marks] Describe an example where theory in algorithmic modelling led to an important advance. |
| *(section 7.2 Theory in algorithmic modeling)*  Informative bounds on the generalization error of classification algorithms depends on the “capacity” of the algorithm. These theoretical bounds led to support vector machines which have proved to be more accurate predictors in classification and regression. |
| e) [2 marks] What learning algorithm does Breiman rate as “A+ for prediction” but “F for interpretability”, and what are his reasons? |
| *(section 9.3 Random forest are A+ predictors)*  Random forests.  Because the mechanism for producing a prediction in random forest is difficult to understand. But overall, in the comparison of 18 different classifiers on four data sets, random forest comes 1, 1, 1, 1 for an average rank of 1.0 in terms of rank of accuracy. |
| f) [2 marks] State ‘Occam’s dilemma’ as Breiman describes it. |
| *(section 9 Occam and simplicity vs. accuracy; section 9.4 The Occam dilemma)*  In prediction, accuracy and simplicity are in conflict. Models with great interpretability are usually not good on prediction, and vice versa.  Accuracy generally requires more complex prediction methods. Simple and interpretable functions do not make the most accurate predictors. |
| g) [2 marks] Describe the main symptom of ‘model instability’. |
| *(section 8 Rashomon and the multiplicity of good models)*  Instability occurs when there are many different models crowded together that have about the same training and test set error. Then a slight perturbation of the data or in the model construction will cause a skip from one model to another. The two models are close to each other in terms of error, but can be distant in terms of the form of the model. |
| h) [2 marks] What is the ‘straight jacket’ that Breiman claims statisticians are imposing (给…带来麻烦) themselves? Why does it matters? |
| *(section 6 The limitations of data models)*  Straight jacket that Breiman claims, “a priori assumption that the nature would generate the data through a parametric model selected by the statistician can result in questionable conclusions that cannot be substantiated by appeal to goodness-of-fit tests and residual analysis.  It is a limitation of data models as data becomes more complex and data problems become wider.  It matters because it restricts the ability of statisticians to deal with a wide range of statistical problems.  The best solution is that we need a larger set of tools. |